| Topic | Examples of interactive data analysis of seismic records |
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Note: Figure numbers followed in this text by ?? relate to the NMSOP editions 2002 (printed) and 2009 (website). They will be changed when the revised Chapter 11 of NMSOP- 2 becomes available.
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## 1 Introduction

The purpose of this information sheet is to illustrate the steps involved when analyzing seismic records by means of the SEISAN software. Examples are given for local, regional and teleseismic earthquakes. This is done by giving representative screen plots together with explanatory texts that follow the figures.

For details on the SEISAN software the reader is referred to section 11.4.2 (Data Analysis and Seismogram Interpretation - Software for routine analysis - SEISAN) and the references therein. Details of the software commands are not given here, and the reader is referred to the SEISAN manual for details, which can be downloaded either from NMSOP-2 via the link 'Download programs and files' or from ftp://ftp.geo.uib.no/pub/seismo/SOFTWARE/SEISAN/ .

The events are included with the sample data that is available with SEISAN (from version 9.2).

The main background material provided by NMSOP-2 (http://nmsop.gfz-potsdam.de), explaining the methodology behind this information sheet, is:

- CHAPTER 2: Seismic Wave Propagation and Earth Models
- CHAPTER 3: Seismic Sources and Source Parameters
- CHAPTER 5: Seismic Sensors and their Calibration
- CHAPTER 6: Seismic Recording Systems
- CHAPTER 11: Data Analysis and Seismogram Interpretation
- IS 2.1: Standard nomenclature of seismic phases
- IS 3.3: The new IASPEI standards for determining magnitudes from digital data and their relation to classical magnitudes
- IS 11.1: Seismic source location
- IS 11.4: Tutorial for consistent phase picking at local to regional distances
- DS 2.1-2.4: Record examples for local, regional and teleseismic earthquakes and explosions

Note that there are in the following some, only apparent, differences between SEISAN internal nomenclature and procedures and those recommended by the IASPEI standards for measuring magnitudes which do not contradict. While SEISAN mb and IASPEI mb are identical, SEISAN mB corresponds to IASPEI mB_BB. Similarly holds that SEISAN Ms = Ms_20 and MS $=$ Ms_BB. Moreover, IASPEI standards recommend to measure mB_BB and Ms_BB on unfiltered broadband velocity traces, however accompanied by the statement that their passband should cover at least the period range within which these two magnitudes should be measured. SEISAN, however, always deconvolves any given actual record so as to simulate for mB _BB a velocity-proportional broadband response in the period range between 0.2 and 30 s and for Ms _BB a response in the period range between 3 and 60 s . This allows in SEISAN to read the broadband magnitudes also on short-period records, provided that the SNR is sufficient to allow a broadband velocity restitution.

## 2 Analysis of a local earthquake in southern Norway recorded between 50 km and 650 km epicentral distance

The earthquake chosen here as example occurred in southern Norway and was recorded on the Norwegian National Seismic Network operated by the University of Bergen. The event was recorded on a mix of short-period and broadband seismic stations. It was automatically detected and then interactively processed.

The earthquake parameters are:

| Date: | 14 Mar 2012 |
| :--- | :--- |
| Origin time: | $19: 22: 27.9$ <br> $(\mathrm{UTC})$ |
| Latitude: | $59.526^{\circ} \mathrm{N}$ |
| Longitude: | $5.615^{\circ} \mathrm{E}$ |
| Depth: | 13.9 km |
| ML: | 3.4 |

We now show the step-by-step procedure to analyze the earthquake.


Vertical-component traces, unfiltered: Our starting point is a waveform file that is produced by an automatic detection system. No additional information is given, although, depending on the automated processing system, additional information including type of event, location and magnitude may already be available. It is our first task to identify the type of event that is recorded. If the detection is not false, the initial choices are between local, regional and teleseismic event. It may also be possible to identify if the event is likely an explosion based on the characteristics of the waveforms and the pattern of phase arrival times. The above multi-trace plot shows records of a small local earthquake, characterized by the short signal duration of less than about 1 min and a relatively high frequency signal content.

The event is recorded on 13 seismic stations. The numbers on the SEISAN multi-trace plot gives the DC of individual traces on the left and the maximum zero to peak amplitude on the right. The units are counts unless instrument correction is used to compute displacement, velocity or acceleration with the units nm (nanometers $=10^{-9} \mathrm{~m}$ ), $\mathrm{nm} / \mathrm{s}$ and $\mathrm{nm} / \mathrm{s}^{2}$, respectively. Station and component codes are given left of each trace together with the location code and network code. For the first trace, the station is ASK, the component is EHZ (short-period seismometer, with high sampling rate of more than 80 samples per second), the location code is 00 (used to indicate differences between equipment that gives the same component code at the same site, for example an STS2 at 40sps is labeled BHZ. 00 and an STS1 at 20sps is labeled BHZ.10) and the network is NS (indicating who operates the station, in this case NS = Norwegian National Seismic Network). The event is well visible on the short-period seismometer records, which have the component code EHZ. However, it is not seen on the broadband traces, which are labeled HHZ, as this is a small earthquake where the signal content is mostly above 0.5 Hz .


Vertical-component traces, filtered 2-8 Hz: Applying this high-frequency band-pass filter, which suppresses the more long-period microseismic noise in the broadband records, the earthquake is now clearly seen on all the traces. As compared to the previous plot, the time window of signal arrivals has been cut out and the time scale been stretched. With distinct primary P - and secondary S-wave arrivals in this frequency band it is very clear that this is a local earthquake. We can see from the arrival times that the earthquake was closest to station BLS5. In SEISAN we then put this event into the database and start the processing.


Single trace plot of station ASK at epicentral distance of 109 km , unfiltered: In SEISAN, we mostly do the phase picks on single trace plots, like shown here, or on three-component trace plots. For this recording on a short-period seismometer it is not necessary to filter the data in order to pick phase arrivals. The P arrival is marked.


Single-trace plot of station ASK at epicentral distance of 109 km , unfiltered: This is the same station as on the previous plot, but this time we have zoomed in on the P arrival. It is now possible to read the P arrival time more accurately, and we can also identify the polarity of the first arrival, which is compression (upward motion on the vertical component) in this case. The phase arrivals will be used for the earthquake location (see IS 11.1) and the polarity can be used to determine the fault plane solution (see also EX 3.2).


Three-component trace plot of station ASK at epicentral distance of 109 km , unfiltered: We normally read the S arrival on one of the two horizontal channels and not on the vertical as SP conversions may arrive prior to $S$ and result in an incorrect reading of the onset time.


Single-trace plots of station ASK at epicentral distance of 109 km , Wood-Anderson filter: To read the ML amplitude, the instrument response is removed and a filter equivalent to the revised Wood-Anderson seismograph response according to Uhrhammer and Collins (1990) (see also IS 3.3) is applied. The bottom trace is a zoomed-in version of the area between the two vertical lines on the top trace. In SEISAN the amplitude is given in units of nanometer. It is measured peak-to-adjacent trough of the maximum deflection of the seismogram trace, where peak and trough are separated by one crossing of the zero-line (sometimes described as "peak-to-peak amplitude") but stored in the database is peak-to-peak/2 according to the IASPEI (2013) standard. This maximum amplitude is normally read from the $S$ or Lg waves. It is stored as the IAML amplitude phase. 'I' stands for IASPEI standard, assuring that the standard Wood-Anderson filter response and the recommended amplitude measurement procedure has been applied (see IS 3.3), and ' $\mathbf{A}$ ' stands for displacement amplitude in nm . IASPEI standard for ML is to measure A on horizontal components. In Norway, however, it is routine practice to use the vertical component for the amplitude reading of ML and the scale given by Alsaker et al. (1991; see also DS 3.1, Tab. 2). This scale was derived for Norway and scaled so that its results match at 60 km distance with those of the horizontal component California standard formula for equal IAML input (see next figure and recommendations in IS 3.3). The default ML formula implemented in SEISAN is that of Hutton and Boore (1987; see next figure and formula in DS 3.1, Tab. 2), on which also the IASPEI standard formula for ML is based (see IS 3.3). If, however, this default procedure is used in other regions with other attenuation conditions then the calculated Ml values may differ from standard ML. DS 3.1. Table 2, offers several M1 calibration functions for other regions together with comments on their scaling, components to be used and the distance range of their applicability. You may implement in SEISAN either your own properly to the ML standard scaled local calibration function, or, if not yet available, one of those which you believe to match best with the seismotectonic conditions in the area. Note, however, that local M1 data based on not yet tested and proven standard scaling should not be published with the nomenclature for standard ML. That is, why we use in NMSOP Ml as the general nomenclature for local magnitude, and ML only for Ml that has been properly scaled to the new standard. Otherwise, users of local magnitude data do not know whether or not they have been correctly scaled according to the now globally set standard. E.g., according to Braunmiller et al. (2005) (see also section 3.2.9.6 in the forthcoming new Chapter 3) the Ml scales used by various agencies in Southern Germany, France, Italy and Switzerland yield results for equal input data that differ on average between 0.2 to $0.6 \mathrm{~m} . \mathrm{u}$. when scaled to Mw.

Some examples for other regional Ml calibration functions have been plotted in the diagram below. Note that the Alsaker et al. (1991) scale (lowermost full line) for the continental shield areas of Scandinavia and Eurasia reveals significantly lower attenuation when compared with Southern California calibration curves of both Richter (1935) and Hutton and Boore (1987) (see full dot and open dot curves in the Figure below). Accordingly, since properly scaled to the latter at about 60 km epicentral distance, the Alsaker et al. calibration curve yields at several 100 km distance for equal amplitude input data already ML values that are several tenths of magnitude units smaller than those derived by applying the original Richter scale. This difference increases to $1.7 \mathrm{~m} . \mathrm{u}$. at a distance of 1500 km , up to which the Alsaker et al. (1991) scale is defined (although strictly Hutton and Boore (1987) is limited to 600 km ).


We now repeat the same procedure of measuring IAML for the other stations, however show only examples from some selected stations to explain specific aspects of the data processing.


Three-component traces of station BLS5 at epicentral distance of 49 km , unfiltered: Plotted are the three-component broadband traces from the nearest station. P and S arrivals, and the ML amplitude were read. In this case the SNR was high enough so that it was not necessary to filter the broadband recordings to identify the phase arrivals.


Three-component traces of station DOMB at epicentral distance of 342 km , unfiltered: Going to larger distances, the signal amplitudes at higher frequencies decrease relative to the more low-frequency microseismic noise, which peaks around 5 seconds. Here, we would normally filter the traces to read the phase arrivals.


Three-component traces of station DOMB at epicentral distance of 342 km , filtered 3-8 Hz : For this station, it is possible to read besides the larger amplitude P and S arrivals, termed Pg and Sg , additionally the commonly weaker but earlier arrivals Pn and Sn . In SEISAN we generally mark the first P - and S -wave arrivals as P and S , respectively. The location program then determines which phase arrives first. Sometimes, Sn (here marked as ES) is weak and not recognizable in the signal-generated noise of scattered $P$ waves. Then one has to mark Sg as such, since the location program otherwise would use it as the first arriving S ( Sn in this case).

Reading different phases with different take-off angle from the source, such as $\mathrm{Pg} / \mathrm{Pn}$ and $\mathrm{Sg} / \mathrm{Sn}$, significantly improves the depth determination. However, one should be quite certain that these identifications are correct. This requires fairly clear arrivals, an experienced analyst and that the phases match the solution when locating. For standard nomenclature, nature and travel paths of crustal phases see IS 2.1 and for many more record examples DS 11.1.


Three-component traces of station FOO at epicentral distance of 233 km , filtered 3-8 Hz: This is an example where Sn cannot be read, and S has to be read as Sg .


Single-trace plot of station NSS at epicentral distance of 649 km , filtered 5-10 Hz: Going to larger distances, the P arrival becomes more emergent and would not be read without applying a filter.


Multi-trace plot of all picked channels: At the end we look at all traces with phase onset and amplitude readings to see whether they are consistently picked. We then start locating. Note that there are simple rules of thumb for a first rough estimates of the approximate hypocenter distance, d, from identified first onsets of P and S waves. If these are Pg and Sg , then it holds $\mathrm{d}[\mathrm{in} \mathrm{km}]=(\mathrm{Sg}-\mathrm{Pg})[\mathrm{in} \mathrm{s}] \times 8$ and in the case of Pn and $\mathrm{Snd}=(\mathrm{Sn}-\mathrm{Pn}) \times 10$. More accurately, the multiplication factor depends on the average P and S wave crustal velocities [see eq. (3) in EX 11.1]: $d=t\left(S_{g}-P_{g}\right)\left(v_{p} v_{s}\right) /\left(v_{p}-v_{s}\right)$.

| \# 1 | 14 M | Mar 2012 | 19:22 28 |  | L | 59.526 | 5.61513 .9 |  | 0.43 3.4BER 12 |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| date hrmn |  | sec | lat |  | long depth |  |  | no m | rms | damp erln erlt |  | erdp |  |
| 12314 | 1922 | 28.19 | 5931. | . $58 \mathrm{~N} \quad 5$ | 536 | 36.9E 13 | 3.92 | 93 | 0.360 | 0.0004 | . 72.0 | - 3.6 |  |
| stn | dist | azm | ain | w phas |  | calcph | hrmn | tsec | t-obs | t-cal | res |  | di |
| BLS5 | 49 | 103.3 | 96.7 | 0 S |  | SG | 1922 | 42.3 | 14.14 | 14.18 | -0.04 | 1.00 | 7 |
| BLS5 | 49 | 103.3 | 96.7 | 0 P | D | PG | 1922 | 36.4 | 8.15 | 8.15 | 0.00 | 1.00 | 4 |
| BLS5 | 49 | 103.3 |  | 0 IAML |  |  | 1922 | 42.5 | 14.3 |  |  |  |  |
| BLS5 | 49 | 103.3 |  | 0 AMPG |  |  | 1922 | 36.4 | 8.2 |  |  |  |  |
| BLS5 | 49 | 103.3 |  | 0 AMSG |  |  | 1922 | 42.4 | 14.2 |  |  |  |  |
| ODD1 | 71 | 52.6 | 93.0 | 0 S |  | SG | 1922 | 48.0 | 19.81 | 20.02 | -0.21 | 1.00 |  |
| ODD1 | 71 | 52.6 | 93.0 | 0 P |  | PG | 1922 | 39.8 | 11.54 | 11.51 | 0.04 | 1.00 | 1 |
| ODD1 | 71 | 52.6 |  | 0 IAML |  |  | 1922 | 48.3 | 20.1 |  |  |  |  |
| BER | 97 | 350.7 | 91.8 | 0 S |  | SG | 1922 | 55.0 | 26.75 | 26.70 | 0.05 | 1.00 | 4 |
| BER | 97 | 350.7 | 91.8 | 0 P |  | PG | 1922 | 43.4 | 15.22 | 15.35 | -0.12 | 1.00 | 2 |
| BER | 97 | 350.7 |  | 0 IAML |  |  | 1922 | 56.9 | 28.7 |  |  |  |  |
| ASK | 109 | 347.7 | 91.5 | 0 S |  | SG | 1922 | 57.7 | 29.52 | 29.95 | -0.43 | 0.98* | 4 |
| ASK | 109 | 347.7 | 91.5 | 0 P |  | PG | 1922 | 45.3 | 17.06 | 17.21 | -0.15 | 0.98* |  |
| ASK | 109 | 347.7 |  | 0 IAML |  |  | 1922 | 59.4 | 31.2 |  |  |  |  |
| SUE | 177 | 344.9 | 90.8 | 0 Sg |  | SG | 1923 | 16.2 | 48.02 | 47.82 | 0.20 | 0.87* |  |
| SUE | 177 | 344.9 | 55.1 | 0 P |  | PN4 | 1922 | 53.8 | 25.56 | 25.93 | -0.37 | 0.87* | 4 |
| SUE | 177 | 344.9 | 90.8 | 0 Pg |  | PG | 1922 | 55.8 | 27.61 | 27.49 | 0.13 | 0.87* | 2 |
| SUE | 177 | 344.9 |  | 0 IAML |  |  | 1923 | 17.7 | 49.5 |  |  |  |  |
| HYA | 185 | 9.4 | 55.1 | 0 S |  | SN4 | 1923 | 16.1 | 47.86 | 46.91 | 0.95 | 0.86* |  |
| HYA | 185 | 9.4 | 90.7 | 0 Sg |  | SG | 1923 | 19.0 | 50.78 | 50.00 | 0.78 | 0.86* | 3 |
| HYA | 185 | 9.4 | 55.1 | 0 P |  | PN4 | 1922 | 55.3 | 27.11 | 26.96 | 0.15 | 0.86* | 2 |
| HYA | 185 | 9.4 |  | 0 IAML |  |  | 1923 | 20.1 | 51.9 |  |  |  |  |
| HYA | 185 | 9.4 | 90.7 | 0 Pg |  | PG | 1922 | 57.1 | 28.85 | 28.74 | 0.12 | 0.86* | 0 |
| HOMB | 217 | 128.8 | 90.6 | 0 Sg |  | SG | 1923 | 26.8 | 58.57 | 58.49 | 0.08 | 0.80* | 6 |
| HOMB | 217 | 128.8 | 90.6 | 0 Pg |  | PG | 1923 | 2.1 | 33.86 | 33.62 | 0.25 | 0.80* | 4 |
| HOMB | 217 | 128.8 |  | 0 IAML |  |  | 1923 | 27.2 | 59.0 |  |  |  |  |
| HOMB | 217 | 128.8 | 55.1 | 0 P |  | PN4 | 1922 | 59.4 | 31.24 | 30.96 | 0.28 | 0.80* | 6 |
| KONO | 225 | 84.8 | 55.1 | 0 P |  | PN4 | 1923 | 0.3 | 32.12 | 31.95 | 0.17 | 0.79* | 3 |
| KONO | 225 | 84.8 | 90.6 | 0 Pg |  | PG | 1923 | 2.9 | 34.70 | 34.81 | -0.11 | 0.79* | 1 |
| KONO | 225 | 84.8 | 90.6 | 0 Sg |  | SG | 1923 | 28.5 | 60.31 | 60.58 | -0.26 | 0.79* | 5 |
| KONO | 225 | 84.8 |  | 0 IAML |  |  | 1923 | 30.2 | 62.0 |  |  |  |  |
| FOO | 233 | 352.5 | 90.6 | 0 Sg |  | SG | 1923 | 30.7 | 62.45 | 62.57 | -0.12 | 0.78* | 2 |
| FOO | 233 | 352.5 | 55.1 | 0 P |  | PN4 | 1923 | 0.9 | 32.71 | 32.88 | -0.17 | 0.78* | 2 |
| FOO | 233 | 352.5 | 90.6 | 0 Pg |  | PG | 1923 | 3.9 | 35.69 | 35.96 | -0.27 | 0.78* | 1 |
| FOO | 233 | 352.5 |  | 0 IAML |  |  | 1923 | 32.5 | 64.3 |  |  |  |  |
| DOMB | 342 | 32.3 | 55.1 | 0 S |  | SN4 | 1923 | 48.1 | 79.93 | 80.82 | -0.89 | 0.60* | 6 |
| DOMB | 342 | 32.3 | 90.4 | 0 Sg |  | SG | 1923 | 59.5 | 91.25 | 91.28 | -0.03 | 0.60* | 3 |
| DOMB | 342 | 32.3 | 55.1 | 0 P |  | PN4 | 1923 | 14.9 | 46.70 | 46.45 | 0.26 | 0.60* | 1 |
| DOMB | 342 | 32.3 | 90.4 | 0 Pg |  | PG | 1923 | 20.6 | 52.35 | 52.46 | -0.11 | 0.60* | 0 |
| MOL | 355 | 16.3 | 55.1 | 0 P |  | PN4 | 1923 | 15.4 | 47.23 | 48.03 | -0.80 | 0.57* |  |
| MOL | 355 | 16.3 |  | 0 IAML |  |  | 1924 | 8.9 | 100.7 |  |  |  |  |
| NSS | 649 | 28.0 | 53.1 | 0 P |  | PN5 | 1923 | 52.6 | 84.43 | 83.82 | 0.61 | 0.08* | 0 |
| ODD1 E | EZ | hdist: |  | 72.6 | amp | p: | 4529 | 9.1 T: | 0.4 | $\mathrm{ml}=$ | 3.7 |  |  |
| BER Hz | HZ | hdist: |  | 97.8 | amp | p: | 1863 | 3.0 T: | 0.4 | $\mathrm{ml}=$ | 3.5 |  |  |
| ASK EZ | EZ | hdist: |  | 109.9 | amp | p: | 2311 | 1.9 T : | 0.1 | $\mathrm{ml}=$ | 3.6 |  |  |
| SUE Hz | HZ | hdist: |  | 177.5 | amp | p: | 1124 | 4.8 T : | 0.1 | $\mathrm{ml}=$ | 3.6 |  |  |
| HYA EZ | EZ h | hdist: |  | 185.5 | amp | p: | 629 | 9.6 T: | 0.4 | $\mathrm{ml}=$ | 3.4 |  |  |
| HOMB Hz | HZ | hdist: |  | 218.4 | amp | p: | 1355 | 5.1 T: | 0.4 | $\mathrm{ml}=$ | 3.8 |  |  |
| KONO B | BZ | hdist: |  | 225.4 | amp | mp: | 144 | 4.8 T : | 0.2 | $\mathrm{ml}=$ | 2.8 |  |  |
| MOL HZ | HZ | hdist: |  | 355.3 | amp | mp: | 112 | 2.3 T : | 0.1 | $\mathrm{ml}=$ | 3.0 |  |  |
| FOO Hz | HZ | hdist: |  | 233.4 | amp | p: | 388 | . 3 T : | 0.4 | $\mathrm{ml}=$ | 3.3 |  |  |
| BLS5 Hz | HZ | hdist: |  | 50.9 | amp | p: | 6142 | 2.4 T: | 0.1 | $\mathrm{ml}=$ | 3.7 |  |  |
| BLS5 Hz | HZ | gdist: |  | 50.9 | mom | m: |  | 3.5 m | mw = | 2.9 |  |  |  |
| FOO Hz | HZ | gdist: |  | 231.4 | mom |  |  | 3.6 m | mw = | 3.0 |  |  |  |
| Number | r of | spectra | avai | ilable a | and | number | used i | in ave | rage | 2 | 2 |  |  |
| 2012 | 314 | 192228 | . 2 L | 59.526 | 6 | 5.615 | 3.9 B | BER 12 | 0.43. | .4LBER 3 | . OWBER |  |  |

Output from location program: We use a standard linearized inversion program (HYPOCENTER, Lienert et al. $(1986,1995)$ ) to locate the event that makes use of the common seismic phases at local distances. The location program tries to minimize the differences between the observed ( $\mathrm{t}-\mathrm{obs}$ ) and calculated arrival times ( $\mathrm{t}-\mathrm{cal}$ ) that are computed for a 1D layered model. The residuals are given in the column labeled 'res'. For our example event these travel-time residuals are relatively small. Note that for station DOMB the residuals are given for both $\mathrm{Pn} / \mathrm{Pg}$ and $\mathrm{Sn} / \mathrm{Sg}$ and that our interpretation fits the solution.

Direct ( Pg and Sg ) and critically refracted wave types ( Pn and Sn ) were very clearly visible from this earthquake on the records of several stations. This helped to constrain the earthquake depth, which was estimated to be 13.9 km (see last but one line). At the end the location procedure the program gives the magnitude values for the individual components and stations, and calculates the average, which is 3.4 in this case. The text 'LBER' refers to the magnitude type ( L for ML ) and the reporting agency $(\mathrm{BER}=$ Bergen $)$. Some spread in the magnitude residuals (difference between single-component magnitude and average) is expected and mostly due to local site effects. In our case the largest residual are -0.6 and +0.4 magnitude units.

A number of polarities were read, 7 compressional (C) and 4 dilatational (D), which are given in the column after the phase name read and the phase used by the location program. For example, in the second phase line of the location output for stations BLS5, the first phase arrival was read as P , the location program decides that this is the direct Pg arrival based on the hypocentral distance. The polarity is read as D , standing for down or dilatation. The location program computes the azimuth (azm) and angle of incidence (ain), which in this example are $103.3^{\circ}$ and $96.7^{\circ}$, respectively. The polarity data can be used to determine the fault plane solution if there are sufficient observations. In this example we can not find a robust solution and do not show the procedure here.

The velocity model used is given by the following table:

| Depth of top of layer in $\mathbf{~ k m}$ | $P$-wave velocity in $\mathbf{~ k m} / \mathbf{s}$ |
| :---: | :---: |
| 0 | 6.2 |
| 12 | 6.6 |
| 23 | 7.1 |
| 31 | 8.05 |
| 50 | 8.25 |
| 80 | 8.5 |



Wadati diagram: To check our readings we can plot the Wadati diagram (plotting S-P times against absolute P arrival times (labels on x -axis given to show scaling), and the data points should fall onto a line like in this example. Data points $(+)$ that are significantly off the line should be checked and re-read.


Travel time plot: We can also produce a simple travel-time plot that shows the observations $(+)$ together with the calculated travel-time curves for P and S first arrivals according to the local velocity model implemented in the SEISAN location program (solid lines). For distances greater than about 150 km , our Pg (around the lower curve) and Sg arrivals (around the upper curve) come in mostly after the predicted first arrivals.

Note that SEISAN uses layered 1D velocity models and the user needs to enter the model for his or her respective area. SEISAN allows the use of a number of 1D models for events depending on their location to account for changes in structure within the area of interest or network coverage.


Source spectrum plot for station BLS5 at epicentral distance of 49 km : We compute the source displacement spectrum (upper curve in the bottom diagram above the noise spectrum) for the vertical component of this station. The spectrum is corrected for attenuation, which for Norway is given by $Q(f)=440 \times f^{0.7}$ (see data at bottom right). From the spectrum we can approximately read the long-period spectral level, which is translated via the assumed velocity and density model into seismic moment (here $\log _{10} \mathrm{M}_{0}=13.47 \mathrm{Nm}$ ) and moment magnitude $\left(\mathrm{M}_{\mathrm{W}}=2.9\right)$. We also measure the corner frequency $\left(\mathrm{f}_{\mathrm{c}}=10.8 \mathrm{~Hz}\right)$, which is translated into stress drop $\Delta \sigma=68.8$ bars $=6.88 \mathrm{MPa}$ using $\Delta \sigma=(7 / 16) \mathrm{M}_{0} / \mathrm{R}^{3}$ (Eshelby, 1957).


Source spectrum plot for station FOO at epicentral distance of 233 km : The spectral analysis is normally done for a number of stations with good SNR. When comparing the results for this station with those of the previous station (BLS5) one finds the difference between the moment magnitudes to be small, but the stress drop difference to be large because of the reading uncertainty in $f_{c}$ and $\Delta \sigma \sim f_{c}^{3}$. (For related formulas and discussions see EX 3.4). At the end, the averages are computed from all observations and standard deviations are calculated.


Location maps in GoogleEarth: SEISAN creates files that make it possible to look at the location with GoogleEarth immediately. The figure on the left shows the epicenter area with the error ellipse plotted as a solid black line. The extent of the 90 percent confidence error ellipse is about 2.5 by 9.0 km . It is also possible to compare the epicenter location to known fault structures. In the case of explosions we try to see if the event is located close to a known mine or quarry.

On the right, we show a more regional GoogleEarth map, which shows the epicenter as a red dot. The stations are color coded depending on their residual from the hypocenter location where green is low residual, yellow is moderate residual and red is high residual (the color levels are configurable). In this example, there are no stations towards the west and southwest of the epicenter and stations are sparse toward the southeast, resulting in an azimuthal gap of 216 degree. This, together with the dominating N-S extension of the Norwegian network causes the much larger location uncertainty in E-W direction (see error ellipse in the left-hand panel). We can also plot the epicenter together with previously located earthquakes.

## 3 Analysis of a regional earthquake recorded at distance between 440 and 2950 km ( $\Delta<30^{\circ}$ )

As an example we have chosen an earthquake that occurred on the Mohns Ridge, offshore northern Norway. The earthquake with a magnitude greater than 6 was large enough to be recorded globally. Here, we process data that were recorded on the Norwegian National Seismic Network operated by the University of Bergen and data provided by IRIS from the Global Seismograph Network (GSN). All data used here was recorded on broadband stations.

The earthquake parameters provided by the USGS are:

| Date: | 24 May 2012 |
| :--- | :--- |
| Origin time: | $22: 47: 46.6$ <br> $($ UTC ) |
| Latitude: | $72.99^{\circ} \mathrm{N}$ |
| Longitude: | $5.65^{\circ} \mathrm{E}$ |
| Depth: | 8.8 km |
| Mw: | 6.2 |

We now show the step-by-step procedure to analyze the earthquake.


Vertical component multi-trace plot, unfiltered: On the seismograms we clearly see longperiod surface waves, with large amplitudes and pronounced dispersion. This indicates that the earthquake is relatively large and shallow. For the stations, where we see the first arriving P as well we can estimate the approximate distance from the time difference between the P and the Rayleigh surface wave maximum (which is most pronounced in vertical component records). For station BFO this time difference is about 10 min . According to Table 1 below this means that station BFO is about 20 to $25^{\circ}$ degrees away ( $1^{\circ}=111.2 \mathrm{~km}$ ) from the epicenter. Being aware of the station locations, considering the pattern of arrival times, and,
if three-component records are available, also of the first-motion polarity patterns and the better constraining S-P travel-time differences, we can also get a first guess of the epicenter location (see EX 11.2).

Table Approximate time interval $\left(\mathrm{t}_{\mathrm{Rmax}}-\mathrm{t}_{\mathrm{P}}\right)$ between the arrival of the maximum Rayleigh wave amplitude and the first onset of P waves as a function of epicentral distance $\Delta$ according to Archangelskaya (1959) and Gorbunova and Kondorskaya (1977) for dominatingly continental travel paths.

| $\Delta^{\circ}$ | $\mathbf{t}_{\mathbf{R m a x}}-\mathbf{t}_{\mathbf{P}}$ <br> $(\min )$ | $\Delta^{\circ}$ | $\mathbf{t}_{\mathbf{R m a x}}-\mathbf{t}_{\mathbf{P}}$ <br> $(\min )$ | $\Delta^{\circ}$ | $\mathbf{t}_{\mathbf{R m a x}}-\mathbf{t}_{\mathbf{P}}$ <br> $(\min )$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 10 | $4-5$ | 55 | 26 | 100 | $45-46$ |
| 15 | $6-8$ | 60 | $28-29$ | 105 | $47-48$ |
| 20 | $9-10$ | 65 | 31 | 110 | $48-50$ |
| 25 | $10-12$ | 70 | 33 | 115 | 53 |
| 30 | $13-14$ | 75 | 35 | 120 | 55 |
| 35 | $15-16$ | 80 | 37 | 125 | 57 |
| 40 | $18-19$ | 85 | $39-40$ | 130 | 60 |
| 45 | 21 | 90 | 42 | 140 | 64 |
| 50 | 24 | 95 | 43 | 150 | 70 |



Vertical component multi-trace plot, filtered $0.01-0.1 \mathrm{~Hz}$ : Filtering the data at low frequencies, we see both body and surface waves. However, the seismograms are dominated by the surface waves as they have larger amplitudes in this frequency range. The shape of the surface wave trains depends on the Earth structure along the paths (see, e.g., Chapter 2, Figs. 2.10, 2.12 and 2.13) and, because of the dispersion, i.e., the dependence of the surface-wave velocity on the period, also on the epicentral distance (see Figure above). The seismograms also depend on the mechanism of faulting.


Multi-trace plot, filtered 1-5 Hz: Looking at higher frequencies, the surface waves disappear from the seismogram and we look at P and (at these high frequencies and in vertical component records usually less clear) S body waves. If the first arriving P and S phases are Pn and Sn , respectively, then there is a simple "rule of thumb" to estimate the hypocenter distance, namely time difference $\mathrm{Sn}-\mathrm{Pn}[\mathrm{in} \mathrm{s}] \times 10$. For station LOF with a time difference of about 1 min this means a distance of $\approx 600 \mathrm{~km}$, This agrees with the rough estimate from the time difference between the Rayleigh-wave maximum and the P first arrival. On some stations (STEI, TRO and LOF) we can also see a signal in this frequency range arriving much later (about 5 minutes after P for station TRO). This is the T (tertiary)-wave, generated by an earthquake in or near the oceans, propagating in the oceans as an acoustic wave and converted back to seismic wave at the ocean-land boundary near the recording site. (for more explanations see Chapter 2, section 2.6.5). It should not be mistaken for another event.


Three-component traces of station SPAO at epicentral distance of 648 km , unfiltered: Zooming around the P arrival the phase can be picked with or without filter. The error on the phase reading here may be as large as 0.5 sec .


Three-component traces of station LOF at epicentral distance of 603 km , filtered 1-5 Hz : Looking at this coastal station, we clearly see the arrival of the T wave. The amplitude of the T wave is in this case comparable to the S-wave amplitude. According to the time difference (S-P) $[$ in s$] \times 10$ the station is about 600 km away from the source.


All vertical traces, unfiltered: The traces are sorted by distances and the P arrival picks are shown. This type of plot is useful to check the consistency of the picks. Based on the P arrival times, the epicenter is estimated at $73.055^{\circ} \mathrm{N}$ and $5.856^{\circ} \mathrm{E}$. The hypocenter depth is not constrained by the data and given as 0 km by the location program. On stations like SPA0 we can see that we have both high and low frequency. Towards larger distances the high frequencies get attenuated more strongly than lower frequency signals.


All vertical traces, filtered 3-8 Hz: We can see that the signal amplitude of the higher frequencies decreases as we go to larger distances due to attenuation. The distance range here is approximately 440 km (station BJO1) to 2960 km (station ARU).


Selected vertical traces, filtered 2-6 Hz: Computed Pn and Sn phase arrival times have been marked by red vertical lines and the text ' yPn ' and ' ySn '. No S-waves are recognizable in the records of the two stations BJO1 and HSPB closer to the epicenter. They are likely situated in an azimuth range of minimum S-wave and strong P-wave radiation (see EX 3.2). While S appears at larger distances, the phase is emergent and from this plot its travel-time does not match well with the global velocity model used (IASP91). The earthquake is located on the Mid-Atlantic Ridge. The seismograms are complicated both due to source and path effects, including the transition from oceanic to continental crust. The display of theoretical arrivals should only serve as a guide on whether the considered phase is plausible to arrive in this time window. However, it would be wrong to pick a phase close to the predicted time if there is no visible change in the signal.


Three-component trace plot of station MOR8 at epicentral distance of 813 km , filtered 1-5 $H z$ : This is an example where the S arrival can be read quite well on one of the horizontal channels.


Vertical-component trace of station $\operatorname{ARU}\left(\Delta=26.7^{\circ}\right)$, mb filter: While it is possible to read ML amplitudes from this earthquake for stations within about 1500 km , this is not done because the ML scale for Norway is not appropriate for sources on the Mid-Atlantic Ridge. We, therefore, read amplitudes for the teleseismic magnitudes which can be used down to distances of $20^{\circ}$ and even down to $2^{\circ}$ for standard Ms_BB. Moment magnitude for this event can be measured using either regional or teleseismic moment tensor inversion (USGS Mw = 6.2). The plot above shows the mb amplitude reading for station ARU. This is done by deconvolving the broadband instrument response and applying a filter to simulate the WWSSN short-period seismograph (see IS 3.3). The simulation trace is displayed on the bottom trace for the time window indicated by the vertical lines on the top trace (raw data). The amplitude IAmb is automatically read between the largest peak and adjacent trough. It is stored as half of this measurement, which is 195.2 nm , together with the related period T of 0.90 s which is twice the time difference between peak and trough.


Vertical-component trace of station $A R U\left(\Delta=26.7^{\circ}\right), m B \_B B$ filter: This plot shows the mB _ BB amplitude reading made for station ARU. This is done by deconvolving the actual instrument response to a broadband velocity response and reading the velocity amplitude on the simulation trace which is displayed on the bottom for the time window indicated by the vertical lines on the top trace (raw data). The amplitude is automatically read between peak and trough, and stored as half of this measurement, which is $10131.3 \mathrm{~nm} / \mathrm{s}$ with a period of 7.60 s . The period for mB _BB needs to be within $0.2 \mathrm{~s}<\mathrm{T}<30 \mathrm{~s}$ (see IS 3.3).


Vertical-component trace of station $\operatorname{ARU}\left(\Delta=26.7^{\circ}\right), M s \_20$ filter: This plot shows the Ms_20 amplitude reading made for station ARU. This is done by deconvolving the displacement instrument response and applying a filter to simulate the WWSSN long-period seismograph. The simulation trace is displayed on the bottom for the time window indicated by the vertical lines on the top trace (raw data). The amplitude is automatically read between peak and trough, and stored as half of this measurement, which is 34346.5 nm with a period of 18.06 s . The period for Ms_20 needs to be within $18 \mathrm{~s} \leq \mathrm{T} \leq 22 \mathrm{~s}$.


Vertical-component trace of station $\operatorname{ARU}\left(\Delta=26.7^{\circ}\right), M s \_B B$ filter: This plot shows the Ms_BB amplitude reading made for station ARU. If the primary record is not yet a velocity broadband trace then the latter has to be synthesized by deconvolving the actual instrument response to a broadband velocity response and reading the velocity amplitude on the simulation trace. The latter is displayed on the bottom trace for the time window indicated by the vertical lines on the top trace (raw data). The amplitude is automatically read between the largest peak and adjacent trough, and stored as half of this measurement, which is 16468.0 $\mathrm{nm} / \mathrm{s}$, together with a period of 16.10 s , i.e., twice the time difference between the peak and adjacent trough. The period needs to be within $3 \mathrm{~s} \leq \mathrm{T} \leq 60 \mathrm{~s}$, and thus maybe significantly shorter than for Ms_20 measurement, allowing Ms measurements at distances well below $20^{\circ}$ (down to $2^{\circ}$ ).

Based on these four amplitude and period measurements from station ARU, we can compare the magnitudes to Mw :

| Magnitude scale | Value |
| :--- | :--- |
| Mw (USGS) | 6.2 |
| mb | 5.9 |
| mB_BB | 6.7 |
| Ms_20 | 6.0 |
| Ms_BB | 6.1 |

We see that the values for this size of earthquake around magnitude 6 compare well, with the exception of mB_BB which is on global average about 0.3-0.4 m.u. greater than Mw at Mw $=6.2$ and about $0.6 \mathrm{~m} . \mathrm{u}$ larger than mb .


Vertical-component trace of station TRO at $\Delta=5.3^{\circ}, M s \_B B$ filter: Ms_BB can be used down to distances of $2^{\circ}$. This plot shows the Ms_BB amplitude reading made for station TRO. The amplitude is automatically read between peak and trough, and stored as half of this measurement, which is $108113.5 \mathrm{~nm} / \mathrm{s}$ with a period of 21.92 s . The computed magnitude is $\mathrm{Ms} \_\mathrm{BB}=5.7$, compared to $\mathrm{Ms} \_\mathrm{BB}=6.1$ for station ARU.


Output from location program: We use the same standard linearized inversion program (HYPOCENTER) to locate this event as used for the local event. The location is based on the IASP91 global travel-time model. The residuals are much larger than for the local event as the difference between the true regional model and IASP91 is significant. The largest residual here is more than 3 seconds. In the hypocenter determination we fixed the depth to 8.8 km and, using both P and S readings, we obtain a latitude of $72.943^{\circ} \mathrm{N}$ and longitude of $6.096^{\circ} \mathrm{E}$. This compares to $73.055^{\circ} \mathrm{N}$ and $5.856^{\circ} \mathrm{E}$ for the preliminary location based on P arrivals only. The solution based on P and S is 15 km east of the USGS solution.

Based on all our amplitude and period measurements the following network average magnitude values were calculated:

| Magnitude scale | Value |
| :--- | :--- |
| Mw (USGS) | 6.2 |
| mb (USGS) | 5.7 |
| mb | 6.4 |
| mB _BB | 7.0 |
| Ms_20 | 6.3 |
| Ms_BB | 6.1 |

Note that Ms_20 and Ms_BB are within 0.1 m.u. of the USGS Mw. In contrast, both our mb and mB _ BB are significantly larger, with mb , based on only 4 measurements in the near teleseismic distance range between 2000 and 3000 km , even by $0.7 \mathrm{~m} . \mathrm{u}$. larger than USGS mb , based on 299 measurements at a much larger range of distances up to about $11,000 \mathrm{~km}$. This may hint to larger calibration uncertainties of the Gutenberg-Richter (1956) Q function in the near teleseismic distance range, where wave propagation is largely influenced by the greater inhomogeneity of upper mantle wave propagation and attenuation. This may result in larger uncertainty of body-wave magnitude estimates, if they are available in only very limited number in the near teleseismic range. On the other hand, this earthquake has taken place on the North-Atlantic Ridge (see Google map below). Intra-oceanic ridge strike-slip earthquakes are often high stress drop events characterized by a much larger than average ratio of $\mathrm{E}_{\mathrm{S}} / \mathrm{M}_{0}$ and thus much larger Me than Mw (e.g. Bormann and Di Giacomo, 2011; Choy, 2012, in IS 3.5). Then, mb and mB _BB may be much larger than usual too in their relation to long-period Mw and Ms. Therefore one might consider this as an alternative explanation, which is, however, neither supported by the much more representative USGS mb value (being rather normal for $\mathrm{Mw}=6.2$ ) nor by the relatively long and not very impulsive P waveforms. The latter are, in the case of high stress drop events, expected to be relatively short, impulselike and of more high-frequency content (e.g., Fig. 3.6 in Chapter 3). Instead, the P-wave group is rather long for an Mw6.2 event, almost one minute, and relatively long-period.


Location map in GoogleEarth: This map shows the location with its error ellipse on the MidAtlantic ridge and the stations that were used for the analysis and location.

## 4 Analysis of a shallow earthquake recorded at teleseismic distances $\left(30^{\circ}<\Delta<90^{\circ}\right)$

The earthquake chosen here as an example occurred in Russia at a shallow depth of 10 km (according to USGS). We extracted data from IRIS that was recorded on the Global Seismograph Network (GSN). All data used here were recorded on broadband stations.

The earthquake parameters provided by the USGS are:

| Date: | $14 / 02 / 2013$ |
| :--- | :--- |
| Origin time: | $13: 13: 53.1$ (UTC) |
| Latitude: | $67.61^{\circ} \mathrm{N}$ |
| Longitude: | $142.60^{\circ} \mathrm{W}$ |
| Depth: | 10 km |
| Mw: | 6.9 |

We now show the step-by-step procedure to analyze the earthquake.


Multi-trace plot of vertical components, unfiltered: Record durations up to about 60 minutes at some stations and the observation of much larger surface-wave than body wave amplitudes hints to a large shallow earthquake at teleseismic distances.


Vertical-component trace of station $A N M O$ at $\Delta=65.4^{\circ}$, unfiltered (top) and filtered 1-5 Hz (bottom): We start by reading the P arrivals that are very clear for this event. They can be read both on unfiltered (top) and high-pass filtered seismograms (bottom).


Output from the location program: Locating with the first P arrivals only, we obtain an epicenter location $\left(67.522^{\circ} \mathrm{N}, 142.826^{\circ} \mathrm{W}\right)$ and depth $=0 \mathrm{~km}$ that is very close to the one given by the USGS. The depth is not constrained with the teleseismic P arrivals only.


Multi-trace plot of vertical components, unfiltered: Plotted are the traces on which we have read the initial P. Based on the hypocenter obtained, we compute the synthetic arrival times of all phases. The traces are sorted by distance. The phases PP, S and SS are clear on all traces. We will now read the onset times of all these phases (plus P-wave first motion polarity), run the location program again with this additional information and see how the location changes.


Three-component trace plot of station PASC at $\Delta=62.2^{\circ}$, unfiltered: For this station P on the vertical component and S on the N component are very clear. Other phases are not very clear. Note that we do not pick the onsets at the calculated arrival times (red bars) but only at the distinct onset of the real phases with large SNR (black bars).


Three-component trace plot of station PFO at $\Delta=63.3^{\circ}$, filtered $0.02-0.1 \mathrm{~Hz}$ : At this distance there is sufficient separation between S and SKSac to read both phases. The component codes of the horizontal components here are BH 1 and BH 2 to indicate that the instrument is not exactly aligned with the geographic directions. In this case, the direction of orientation is given with the component's metadata and can be used to rotate into a NS-EW system.

| \# 1 | 14 Fe | eb 2013 | 13:13 | 351 D | 67.522142 .826 |  |  | 0.9 |  | TES |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| date | hrmn | sec |  | lat | long dep | pth n | no m | rms | damp | erln | n erlt | erdp |  |
| 13214 | 1313 | 54.89 | 6748. | 67N 142 | 10.4E | 0.15 | 553 | 5.940 | 0.0009 | 92. | 744.2 | 39.3 |  |
| stn | dist | azm | ain | w phas | calcph | s hrmn | tsec | t-o.bs | t-cal |  | res |  | di |
| MAJO | 3485 | 186.1 | 42.8 | 0 PP | PnPn | 1321 | 22.8 | 447.91 | 445.00 |  | 2.91 | 1.00 | 4 |
| MAJO | 3485 | 186.1 | 27.3 | 0 P | P | 1320 | 10.0 | 375.15 | 382.25 |  | -7.11 | 1.00 | 2 |
| MAJO | 3485 | 186.1 | 28.1 | 0 S | S | 1325 | 19.8 | 684.86 | 691.48 |  | -6.62 | 1.00 | 6 |
| KURK | 3858 | 273.1 | 26.8 | 0 P | P | 1320 | 45.3 | 410.38 | 411.44 |  | -1.06 | 1.00 | 1 |
| KURK | 3858 | 273.1 | 40.6 | 0 PP | PnPn | 1322 | 2.6 | 487.69 | 487.73 |  | -0.04 | 1.00 | 3 |
| KURK | 3858 | 273.1 | 27.7 | 0 S | S | 1326 | 18.9 | 744.06 | 743.37 |  | 0.69 | 1.00 | 4 |
| MAKZ | 4072 | 266.2 | 26.4 | 0 P | P | 1321 | 1.0 | 426.08 | 428.05 |  | -1.98 | 1.00 | 1 |
| MAKZ | 4072 | 266.2 | 39.7 | 0 PP | PnPn | 1322 | 27.4 | 512.54 | 511.60 |  | 0.94 | 1.00 | 2 |
| MAKZ | 4072 | 266.2 | 46.9 | 0 SS | SnSn | 1329 | 16.4 | 921.49 | 924.72 |  | -3.23 | 1.00 | 9 |
| XAN | 4308 | 226.6 | 25.9 | 0 P | P | 1321 | 18.1 | 443.21 | 446.13 |  | -2.92 | 1.00 | 0 |
| XAN | 4308 | 226.6 | 34.8 | 0 PP | PP | 1322 | 52.7 | 537.78 | 535.32 |  | 2.46 | 1.00 | 1 |
| XAN | 4308 | 226.6 | 27.1 | 0 S | S | 1327 | 16.3 | 801.38 | 805.45 |  | -4.08 | 1.00 | 2 |
| ENH | 4687 | 224.0 | 25.2 | 0 P | P | 1321 | 45.2 | 470.34 | 474.30 |  | -3.96 | 1.00 | 0 |
| ENH | 4687 | 224.0 | 34.3 | 0 PP | PP | 1323 | 30.7 | 575.79 | 572.36 |  | 3.43 | 1.00 | 1 |
| ENH | 4687 | 224.0 | 26.5 | 0 S | S | 1328 | 6.2 | 851.27 | 856.26 |  | -4.99 | 1.00 | 2 |
| ENH | 4687 | 224.0 | 36.7 | 0 SS | SS | 1331 | 20.01 | 1045.071 | 1046.08 |  | -1.01 | 1.00 | 3 |
| TATO | 4960 | 207.1 | 24.6 | 0 P | P | 1322 | 5.6 | 490.73 | 494.12 |  | -3.39 | 1.00 | 1 |
| TATO | 4960 | 207.1 | 33.8 | 0 PP | PP | 1323 | 57.4 | 602.48 | 598.76 |  | 3.72 | 1.00 | 2 |
| tato | 4960 | 207.1 | 26.0 | 0 S | S | 1328 | 43.4 | 888.52 | 892.20 |  | -3.68 | 1.00 | 3 |
| LSA | 5373 | 244.7 | 23.7 | 0 P | P | 1322 | 38.1 | 523.17 | 523.96 |  | -0.80 | 1.00 | 0 |
| LSA | 5373 | 244.7 | 28.4 | 0 PP | PP | 1324 | 35.9 | 641.06 | 636.87 |  | 4.19 | 1.00 | 1 |
| LSA | 5373 | 244.7 | 25.3 | 0 S | S | 1329 | 40.4 | 945.49 | 946.59 |  | -1.10 | 1.00 | 1 |
| LSA | 5373 | 244.7 | 29.2 | 0 SS | SS | 1333 | 24.01 | 1169.111 | 1158.32 |  | 10.78 | 1.00 | 2 |
| COR | 5690 | 66.0 | 23.1 | 0 P | P | 1322 | 57.4 | 542.53 | 545.00 |  | -2.47 | 1.00 | 1 |
| COR | 5690 | 66.0 | 24.7 | 0 S | S | 1330 | 21.9 | 986.97 | 985.30 |  | 1.67 | 1.00 | 2 |
| COR | 5690 | 66.0 | 28.6 | 0 SS | SS | 1334 | 25.71 | 1230.761 | 1203.01 |  | 27.74 | 1.00 | 3 |
| QIZ | 5870 | 219.4 | 22.7 | 0 P | P | 1323 | 9.3 | 554.36 | 557.21 |  | -2.85 | 1.00 | 0 |
| QIZ | 5870 | 219.4 | 28.1 | 0 PP | PP | 1325 | 15.6 | 680.66 | 677.02 |  | 3.64 | 1.00 | 1 |
| QIZ | 5870 | 219.4 | 24.4 | 0 S | S | 1330 | 41.41 | 1006.491 | 1007.80 |  | -1.32 | 1.00 | 2 |
| QIZ | 5870 | 219.4 | 28.5 | 0 SS | SS | 1334 | 45.31 | 1250.381 | 1228.62 |  | 21.76 | 1.00 | 2 |
| ESK | 6053 | 336.5 | 22.3 | 0 P | P | 1323 | 23.0 | 568.08 | 568.79 |  | -0.71 | 1.00 | 2 |
| Anto | 6707 | 303.4 | 20.9 | 0 P | P | 1324 | 5.6 | 610.70 | 610.87 |  | -0.17 | 1.00 | 2 |
| ANTO | 6707 | 303.4 | 27.5 | 0 PP | PP | 1326 | 22.1 | 747.22 | 744.41 |  | 2.81 | 1.00 | 3 |
| ANTO | 6707 | 303.4 |  | 0 |  | 1327 | 47.7 | 832.8 |  |  |  |  |  |
| ANTO | 6707 | 303.4 | 22.8 | 0 S | S | 1332 | 27.01 | 1112.141 | 1107.57 |  | 4.57 | 1.00 | 6 |
| PASC | 6918 | 67.4 | 20.5 | 0 P | P | 1324 | 14.8 | 619.92 | 623.83 |  | -3.91 | 1.00 | 1 |
| PASC | 6918 | 67.4 | 22.4 | 0 S | S | 1332 | 47.81 | 1132.861 | 1131.89 |  | 0.97 | 1.00 | 2 |
| PFO | 7042 | 66.2 | 20.2 | 0 P | P | 1324 | 22.4 | 627.56 | 631.41 |  | -3.85 | 1.00 | 1 |
| PFO | 7042 | 66.2 | 22.2 | 0 S | S | 1333 | 1.51 | 1146.591 | 1146.11 |  | 0.48 | 1.00 | 2 |
| PFO | 7042 | 66.2 | 13.3 | 0 SKSac | SKSac | 1334 | 22.11 | 1227.241 | 1226.38 |  | 0.86 | 1.00 | 1 |
| ANMO | 7276 | 57.2 | 19.7 | 0 P | P | 1324 | 36.6 | 641.73 | 645.27 |  | -3.54 | 1.00 | 1 |
| ANMO | 7276 | 57.2 | 21.7 | 0 S | S | 1333 | 24.01 | 1169.091 | 1172.25 |  | -3.16 | 1.00 | 2 |
| WVT | 7747 | 41.4 | 18.8 | 0 P | P | 1325 | 2.0 | 667.12 | 671.69 |  | -4.57 | 1.00 | 1 |
| WVT | 7747 | 41.4 | 20.8 | 0 S | S | 1334 | 11.71 | 1216.831 | 1222.45 |  | -5.62 | 1.00 | 2 |
| WVT | 7747 | 41.4 | 27.7 | 0 SS | SS | 1338 | 42.61 | 1487.751 | 1492.76 |  | -5.01 | 1.00 | 3 |
| HKT | 8153 | 50.2 | 17.9 | 0 P | P | 1325 | 25.0 | 690.14 | 693.79 |  | -3.65 | 1.00 | 1 |
| HKT | 8153 | 50.2 | 20.0 | 0 S | S | 1334 | 55.21 | 1260.271 | 1264.73 |  | -4.46 | 1.00 | 2 |
| SLBS | 8309 | 64.7 | 17.6 | 0 P | P | 1325 | 33.8 | 698.88 | 702.32 |  | -3.44 | 1.00 | 1 |
| SLBS | 8309 | 64.7 | 19.7 | 0 S | S | 1335 | 15.71 | 1280.781 | 1281.06 |  | -0.29 | 1.00 | 2 |
| SLBS | 8309 | 64.7 | 27.3 | 0 SS | SS | 1340 | 12.21 | 1577.301 | 1570.17 |  | 7.13 | 1.00 | 3 |
| TEIG | 9412 | 46.6 | 15.2 | 0 P | P | 1326 | 27.4 | 752.56 | 755.95 |  | -3.39 | 1.00 | 0 |
| TEIG | 9412 | 46.6 | 25.1 | 0 PP | PP | 1329 | 48.6 | 953.66 | 952.02 |  | 1.64 | 1.00 | 1 |
| CTAO | 9733 | 176.2 | 14.4 | 0 P | P | 1326 | 39.3 | 764.36 | 769.71 |  | -5.35 | 0.00 | 0 |
| CTAO | 9733 | 176.2 | 24.8 | 0 PP | PP | 1330 | 6.6 | 971.71 | 975.50 |  | -3.79 | 1.00 | 2 |
| MTDJ | 9927 | 37.4 | 10.3 | 0 SKSac | SKSac | 1337 | 24.11 | 1409.231 | 1409.91 |  | -0.68 | 1.00 | 1 |
| MTDJ | 9927 | 37.4 | 24.6 | 0 PP | PP | 1330 | 25.7 | 990.79 | 989.60 |  | 1.18 | 1.00 | 1 |
| MTDJ | 9927 | 37.4 | 14.1 | 0 P | P | 1326 | 52.7 | 777.80 | 778.52 |  | -0.72 | 1.00 | 0 |
| 2013 | 2141 | 131354 | 4.9 D | 67.811 | 142.173 | 0.1 T | TES 20 | 05.9 |  |  |  |  |  |

Output from the location program: Using additional phases the location changes slightly, but without readings of depth phases or P-wave onsets very near to this shallow source the depth cannot be better resolved compared to the USGS.


Vertical component traces of stations KBS and KDAK, unfiltered: We try to read first-motion P-wave polarities (upward motion $=\mathrm{C}=+=$ compressional, downward motion $=\mathrm{D}=-=$ dilatational) which can allow us to estimate a fault-plane solution for this earthquake. For station KBS (top) it is possible to read the polarity, which is upward (compression). For station KDAK it is not possible to read the polarity, although we were tempted to read this as a downward motion (dilatation). As seen further down, the selected data set does not have stations that are for sure in a dilatational quadrant, however, the position of all our compressional readings (see next figure) are in agreement with Global CMT fault-plane solution.

The following solution was provided by the Global CMT catalog (www.globalcmt.org) for this event. The solution shows an oblique thrust mechanism:

## 201302141313A EASTERN SIBERIA, RUSSIA

```
Date: 2013/ 2/14 Centroid Time: 13:13:58.6 GMT
Lat= 67.71 Lon= 142.62
Centroid time minus hypocenter time: 5.5
Moment Tensor: Expo=26 1.030 -0.627-0.404 0.335 0.075 0.729
Mw = 6.7 mb = 0.0 Ms = 6.6 Scalar Moment = 1.2e+26
Fault plane: strike=327 dip=42 slip=115
Fault plane: strike=115 dip=52 slip=69
```



Fault-plane solution plot: This plot is created in SEISAN and shows the solution given by the Global CMT catalog together with polarities read from the example. We can see that all our observations lie near the center of the focal sphere and are likely compressions. However, the readings we made show compression and dilatation, and most likely the dilatational readings are wrong. Although looking at more than 100 stations from the global networks, we do not have good enough coverage of the focal sphere as all our rays to teleseismic stations only leave the source downward near the vertical. In contrast, the moment tensor solution (based on full waveforms from $P, S$ and surface waves) normally requires only few stations to obtain a good solution. Using complementary to first-motion polarity readings in SEISAN also S/P amplitude ratios for better constraining fault-plane solutions is possible for local and teleseismic earthquakes. While the use of amplitude ratios did not help with this example, Figure 7.26 in Havskov and Ottemöller (2010) gives an example of teleseismic fault plane solution using amplitude ratios. The polarity readings made by us on individual station records (open circles $=\mathrm{C}$, triangles $=\mathrm{D}$ ) are given on the side with a link to the azimuth and angle of incidence of the corresponding phase projected onto the focal sphere.

Finally, we demonstrate the magnitude determinations for this earthquake:


Traces of station $A N T O$ at $\Delta=60.3^{\circ}, m B \_B B$ filter: First we read amplitudes for mb and mB _BB. Measured are the largest P -wave amplitude prior to PP, depth phases of P included, on the vertical component of simulated short-period WWSSN, respectively velocity broadband records. The position of the earlier Iamb measurement has been plotted here on the mB _ BB filtered trace only for comparison by a red arrow-bar. Details of teleseismic bodywave magnitudes are given in the regional event example in section 3 above and in IS 3.3.


Traces of station ESK at $\Delta=54.4^{\circ}, M s \_B B$ filter: Next we determine the two IASPEI standard surface-wave magnitudes. The bottom trace shows the reading position of the Ms_BB amplitude IVMs_BB (black arrow-bar) on an instrument corrected broadband velocity trace.

The top trace is unfiltered and shows the time selection for the bottom trace. Note that the IAMs_20 amplitude has already been read on another, WWSSN-LP filtered, record, before. However, the position of its measurement is shown here too for comparison (marked by a red arrow-bar). While the largest Ms_20 displacement amplitude has a period of 21 s , the period of the 10.5 min later arriving largest Ms_BB velocity amplitude is 11.80 s only. For more details on the determination of teleseismic surface-wave magnitude see the regional event example in section 3 as well as IS 3.3.

Computing the average magnitudes from all amplitude observations we get the values below:

| Magnitude scale | Value |
| :--- | :--- |
| Mw (USGS) | 6.9 |
| mb | 6.7 |
| mB_BB | 7.3 |
| Ms_20 | 6.9 |
| Ms_BB | 6.9 |

In this case the surface wave magnitudes Ms_20 and Ms_BB agree perfectly with Mw(USGS) and are equal amongst each other although Ms_BB has been measured at a much shorter period and a later time than Ms_20. $\mathrm{mB} \_\mathrm{BB}$ is significantly larger than mb , and somewhat larger than the two Ms and the Mw magnitude, as expected for earthquakes of $\mathrm{Mw}=6.9$ according to Utsu (2002) and Fig. 3.70 in section 3.2.9.1 of the forthcoming revised Chapter $3)$.

The amplitudes and periods that were read for computing the magnitudes are summarized in the following table. Note that here the abridged internal magnitude nomenclature used in SEISAN stands for: $\mathrm{mb}=\mathrm{mb}, \mathrm{mB}=\mathrm{mB} \_\mathrm{BB}, \mathrm{Ms}=\mathrm{Ms} \_20$ and $\mathrm{MS}=\mathrm{Ms}$ _BB.

| XAN | BZ | dist: | 4308.0 | amp: | 1498.7 T: | 1.8 | $\mathrm{mb}=$ | 6.3 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| XAN | BZ | dist: | 4308.0 | amp: | 22757.5 T: | 8.8 | $\mathrm{mB}=$ | 7.0 |
| ENH | BZ | dist: | 4687.0 | amp: | 959.5 T: | 1.5 | mb | 6.3 |
| ENH | BZ | dist: | 4687.0 | amp: | 17567.1 T: | 8.8 | mB | 6.9 |
| ENH | BZ | dist: | 4687.0 | amp: | $120000.0 \mathrm{~T}:$ | 10.9 | $\mathrm{MS}=$ | 7.3 |
| ENH | BZ | dist: | 4687.0 | amp: | $184000.0 \mathrm{~T}:$ | 18.6 | Ms | 7.0 |
| TATO | BZ | dist: | 4960.0 | amp: | 436.4 T: | 0.9 | mb | 6.3 |
| TATO | BZ | dist: | 4960.0 | amp: | 20681.6 T : | 9.0 | mB | 7.2 |
| TATO | BZ | dist: | 4960.0 | amp: | $111000.0 \mathrm{~T}:$ | 18.9 | Ms = | 6.8 |
| TATO | BZ | dist: | 4960.0 | amp: | 81389.9 T : | 11.8 | $\mathrm{MS}=$ | 7.2 |
| COR | BZ | dist: | 5690.0 | amp: | 18587.7 T: | 3.8 | mB | 7.2 |
| COR | BZ | dist: | 5690.0 | amp: | $778.2 \mathrm{~T}:$ | 1.1 | $\mathrm{mb}=$ | 6.5 |
| COR | BZ | dist: | 5690.0 | amp: | 11899.5 T: | 15.7 | MS = | 6.4 |
| COR | BZ | dist: | 5690.0 | amp: | $31700.7 \mathrm{~T}:$ | 18.9 | $\mathrm{Ms}=$ | 6.4 |
| ESK | BZ | dist: | 6053.0 | amp: | 6275.4 T : | 1.1 | $\mathrm{mb}=$ | 7.6 |
| ESK | BZ | dist: | 6053.0 | amp: | $171000.0 \mathrm{~T}:$ | 8.5 | mB | 8.2 |
| ESK | BZ | dist: | 6053.0 | amp: | $336000.0 \mathrm{~T}:$ | 20.8 | $\mathrm{Ms}=$ | 7.4 |
| ESK | BZ | dist: | 6053.0 | amp: | $228000.0 \mathrm{~T}:$ | 11.8 | MS | 7.7 |
| ANTO | BZ | dist: | 6707.0 | amp: | 721.5 T : | 1.2 | $\mathrm{mb}=$ | 6.7 |
| ANTO | BZ | dist: | 6707.0 | amp: | 16728.9 T : | 5.9 | mB | 7.3 |
| ANTO | BZ | dist: | 6707.0 | amp: | 57305.5 T: | 19.2 | Ms = | 6.7 |
| ANTO | BZ | dist: | 6707.0 | amp: | 20010.4 T: | 20.0 | $\mathrm{MS}=$ | 6.8 |
| ANMO | BZ | dist: | 7276.0 | amp: | 9820.2 T : | 3.8 | mB | 7.2 |
| ANMO | BZ | dist: | 7276.0 | amp: | 892.4 T: | 2.0 | $\mathrm{mb}=$ | 6.6 |
| ANMO | BZ | dist: | 7276.0 | amp: | 18195.2 T : | 21.0 | MS | 6.8 |
| ANMO | BZ | dist: | 7276.0 | amp: | 59228.9 T: | 21.3 | $\mathrm{Ms}=$ | 6.8 |
| WVT | BZ | dist: | 7747.0 | amp: | 68435.1 T : | 20.2 | Ms | 6.9 |
| WVT | BZ | dist: | 7747.0 | amp: | 20200.8 T: | 19.0 | $\mathrm{MS}=$ | 6.9 |
| DWPF | BZ | dist: | 8770.0 | amp: | 1956.5 T : | 2.2 | mb | 6.8 |
| DWPF | BZ | dist: | 8770.0 | amp: | $11188.1 \mathrm{~T}:$ | 3.6 | $\mathrm{mB}=$ | 7.1 |
| DWPF | BZ | dist: | 8770.0 | amp: | 74362.7 T: | 22.0 | Ms $=$ | 7.0 |
| DWPF | BZ | dist: | 8770.0 | amp: | 22267.2 T: | 23.6 | $\mathrm{MS}=$ | 7.0 |
| TEIG | BZ | dist: | 9412.0 | amp: | 12224.9 T : | 2.9 | mB | 7.3 |
| TEIG | BZ | dist: | 9412.0 | amp: | 853.1 T : | 1.4 | $\mathrm{mb}=$ | 6.8 |
| TEIG | BZ | dist: | 9412.0 | amp: | 18134.1 T : | 21.4 | $\mathrm{MS}=$ | 7.0 |
| TEIG | BZ | dist: | 9412.0 | amp: | 58385.9 T : | 20.6 | $\mathrm{Ms}=$ | 7.0 |
| CTAO | BZ | dist: | 9733.0 | amp: | 686.2 T : | 2.0 | $\mathrm{mb}=$ | 6.6 |
| CTAO | BZ | dist: | 9733.0 | amp: | 4437.9 T : | 19.5 | $\mathrm{MS}=$ | 6.4 |
| CTAO | BZ | dist: | 9733.0 | amp: | 13972.4 T: | 21.4 | Ms = | 6.3 |



Map showing the epicenter (red star) and stations (blue triangles) used here.

## 5 Analysis of an intermediate depth earthquake at teleseismic distances

The earthquake chosen here as example occurred in Colombia at an intermediate depth of 129 km (depth by USGS). We extracted data from IRIS that were recorded by the Global Seismograph Network (GSN). All data used here were recorded on broadband stations.

The earthquake parameters provided by the USGS are:

| Date: | $09 / 02 / 2013$ |
| :--- | :--- |
| Origin time: | $14: 16: 06.3$ (UTC) |
| Latitude: | $1.14^{\circ} \mathrm{N}$ |
| Longitude: | $77.36^{\circ} \mathrm{W}$ |
| Depth: | 129 km |
| Mw: | 7.0 |

We now show the step-by-step procedure to analyze the earthquake.


Three-component trace plot of station BFO at $\Delta=86.4^{\circ}$, unfiltered: Looking at one of the stations, we can see that we are dealing with an earthquake at teleseismic distance as the record shown extends to almost one hour. The seismograms show very clear body-wave phase arrivals, which we will try to identify. The lack of more long-period and dispersed surface waves, however, points at a deep hypocenter. We will start to pick first P arrivals to get an initial estimate of the location, then we try to identify depth phases and other later phases for improved hypocenter determination and finally we use the 3 -component record of station BFO only for a single-station event location.


Multi-trace plot of vertical components, unfiltered: Shown is only a selection of the stations that are part of the sample data set for this event.


Vertical-component traces for which phases are picked, filtered 0.02-5 Hz: These traces are sorted by epicentral distance, ranging from $30.7^{\circ}$ to $162.7^{\circ}$. Beside the P first arrival, at some of the traces also clear later arrivals have been marked and identified. Note that from station KURK downward the strong delay of the first arriving longitudinal waves is due to the Earth core shadow for direct P waves. In fact, the group of later arrivals, annotated here as P , relate to different branches of PKP core phases and likely also their depth phases. Also note several distinct onsets following within the first minute after the $P$ onset and well before the arrival of PP. For a first event location we will only use the P and PKP first arrivals. Later, we will zoom into the first few minutes of records in order to find depth phases of $P$ and PKP.


Vertical-component trace of station $K D A K$ at $\Delta=81.2^{\circ}$, top unfiltered, bottom filtered 1-5 Hz: Whereas most of the P arrivals in the earlier shown record section of all stations had a good SNR, this is an example where the P arrival can only be picked after filtering the trace. The time window of the expanded lower trace is marked by the vertical lines on the unfiltered top trace. The use of the filter introduces a small phase shift and at some observatories it is common practice to read all stations with the same filter. However, as long as the phase shift is small as compared to the reading error one can, depending on the signal-to-noise ratio (SNR) of individual stations, chose the best filter or no filter. There may also be stations where the SNR is too low and phases will not be read. This is better than reading false phases.

| \# 1 | 9 Feb | eb 2013 | 3 14:1 | 17 | 8 D |  |  |  |  |  |  | ? 1 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| date hrmn |  | sec | lat |  |  | long depth |  | no m | rms | damp erln erlt |  | erdp |
| 1329 | 1416 | 6.75 | 110. | . 98 N | N 77 | 22.6W 13 |  | 193 | 0.64 | 0.0001 | 15.612 .3 | 48.7 |
| stn | dist | azm | ain | w p | phas | calcph | hrmn | tsec | t-o.bs | t-cal | 1 res | wt di |
| LCO | 3417 | 168.5 | 39.7 | 0 P | P | P | 1422 | 9.6 | 362.83 | 362.82 | 20.01 | $1.00 * 17$ |
| RCBR | 4675 | 100.0 | 36.2 | 0 P |  | P | 1423 | 45.0 | 458.23 | 458.28 | $8-0.05$ | 1.00*11 |
| PFO | 5430 | 315.6 | 33.7 | 0 P | P | P | 1424 | 39.4 | 512.70 | 511.80 | $0 \quad 0.90$ | $0.97 * 21$ |
| EFI | 6139 | 165.5 | 31.5 | 0 P |  | P | 1425 | 25.1 | 558.33 | 558.79 | 9-0.47 | 0.99* 9 |
| CMLA | 6665 | 46.1 | 29.8 | 0 P |  | P | 1425 | 59.0 | 592.23 | 591.93 | $3 \quad 0.30$ | 1.00* |
| MACI | 7120 | 59.1 | 28.4 | 0 P |  | P | 1426 | 27.2 | 620.43 | 619.48 | 80.95 | 0.97* 5 |
| PAB | 8482 | 49.6 | 24.3 | 0 P |  | P | 1427 | 40.6 | 693.81 | 694.00 | $0-0.20$ | 1.00* 3 |
| KDAK | 9032 | 328.4 | 22.6 | 0 P |  | P | 1428 | 6.6 | 719.81 | 720.90 | $0-1.09$ | 0.96* 5 |
| BFO | 9603 | 41.8 | 20.8 | 0 P |  | P | 1428 | 32.9 | 746.20 | 747.04 | $4-0.84$ | 0.98* 2 |
| KBS | 9876 | 11.1 | 19.9 | 0 P |  | P | 1428 | 45.8 | 759.07 | 758.66 | $6 \quad 0.41$ | 0.99* 1 |
| KEV | 10448 | 19.8 | 19.4 | 0 P |  | P | 1429 | 8.0 | 781.28 | 782.45 | $5-1.18$ | 0.96* 1 |
| BILL | 10966 | 340.1 | 18.8 | 0 P |  | Pdif | 1429 | 29.2 | 802.41 | 803.17 | $7-0.76$ | 0.98* 2 |
| KURK | 13847 | 18.3 | 8.0 | 0 P |  | PKPdf | 1434 | 49.31 | 1122.541 | 1123.03 | $3-0.49$ | 0.99* 2 |
| NWAO | 16204 | 202.0 | 7.0 | 0 P |  | PKPdf | 1435 | 28.61 | 1161.821 | 1161.84 | $4-0.02$ | 1.00* |
| ENH | 16480 | 348.7 | 6.8 | 0 P |  | PKPdf | 1435 | 33.21 | 1166.431 | 1165.98 | 80.45 | 0.99* 2 |
| KMI | 17127 | 359.8 | 5.9 | 0 P |  | PKPdf | 1435 | 42.81 | 1176.031 | 1175.09 | 90.94 | 0.97* 2 |
| PALK | 17430 | 68.7 | 5.4 | 0 P |  | PKPdf | 1435 | 45.81 | 1179.101 | 1178.53 | $3 \quad 0.57$ | 0.99* 3 |
| CHTO | 17789 | 10.1 | 4.8 | 0 P |  | PKPdf | 1435 | 49.51 | 1182.781 | 1182.46 | $6 \quad 0.32$ | 1.00* 2 |
| KAPI | 18088 | 257.1 | 4.2 | 0 P |  | PKPdf | 1435 | 52.21 | 1185.461 | 1185.29 | 90.16 | 1.00* 3 |
| 2013 | 291 | 14166 | 6.8 D |  | 1.183 | -77.3771 | 2.4 | TES 19 | 90.6 |  |  |  |

Output from the location program on the previous page: Locating with the first P arrivals only, we obtain a hypocenter location $\left(1.183^{\circ} \mathrm{N}, 77.377^{\circ} \mathrm{W}\right.$ and depth $\left.=132.4 \mathrm{~km}\right)$ that is very close to the one given by the USGS. The depth estimate is perhaps better than expected in this case without the use of depth phases. However, we will now try to use the depth phases we noticed on a number of seismograms. We have so far read all first arrivals as P . The location program determines which phase arrives first. In our example we have P (until station KEV), Pdif (station BILL) and PKPdf (from station KURK onward).


Vertical-component trace for station BFO at $\Delta=86.4^{\circ}$, unfiltered: For this station we have computed synthetic arrival times based on our initial location, which are marked with red bars. We can see distinct phases arriving near the computed $\mathrm{pP}, \mathrm{sP}$ and PP times. The bottom trace shows the picking of pP about 4 s after the predicted arrival, but there is no clear new energy arrival around the expected sP onset. Note, however, that sP may sometimes be even a stronger phase than pP . The amplitude relationship between these two depth phases depends on the radiation pattern of the source mechanism, which is different for P and S waves (see Chapter 3, section 3.4.1, Figs. 3.100-104), and on the different take-off angles of pP and sP from the source (see Chapter 2, section 2.6 .3 with figures). From the measured travel-time difference of 38.2 s between pP and P we estimate a source depth of about 150 km , some 20 km deeper than the source depth calculated by the USGS.


Three-component trace of station CHTO at $\Delta=160.0^{\circ}$, unfiltered: Knowing from the first location of the earthquake that the station is $160^{\circ}$ away the first arrival at 35 m 50 s is clearly not $P$, as originally marked, but PKPdf. The larger onset about 5 s later is a second phase of the same event, yet the much stronger sharp wave onset at about 36 m 28 s is obviously the depth phase pPKPdf and the onset at about 36 m 45 s the depth phase sPKPdf. Note that the travel-time difference pPKPdf-PKPdf of 38 s perfectly agrees with the time difference $\mathrm{pP}-\mathrm{P}=$ 38.2 s measured at station BFO. Note that the differential times such as $\mathrm{pP}-\mathrm{P}$ and $\mathrm{sP}-\mathrm{P}$ should be near constant over a distance range.


Vertical-component trace for station KMI at $\Delta=154.0^{\circ}$, unfiltered: In this example we can see onsets that relate to the different travel-time branches of PKP. The corresponding depth phase times are also shown and phases are visible. Core phases are often most clear in the frequency band 1-5 Hz.


Three-component traces for station BILL at $\Delta=98.6^{\circ}$, rotated and filtered 0.01-0.1 Hz: The two horizontal components have been rotated into radial and transverse components using a backazimuth of $65^{\circ}$. SKS has been back-converted from a P wave through the outer core, termed $K$, into an $S$ wave through the mantle and is, therefore, polarised in the vertical plane of propagation. Accordingly, it has its largest amplitude in the radial component R (middle trace) and not on the transverse component T. It is also visible on the vertical component. This is not the rule for teleseismic S and illustrates that rotating seismograms can be useful in identifying seismic phases (see Figs. 11.12, 11.37 and 11.56 ?? in the Manual Chapter 11 of Bormann, 2009). Having an array of stations, the different apparent velocities of seismic phases can also be used for identification (see, e.g., Chapter 9, and for the identification of core phases Fig. 11.34 ?? in the Manual edition by Bormann (2009).

| \# 1 | 9 F | eb 2013 14:16 | 16 | 8 D | 1.008 | 77.514 | 4150.1 |  | 36.8 bTE | S 19 | ? 1 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| date | hrmn |  | lat |  | long depth |  | $\begin{array}{ll} \text { no } & \mathrm{m} \\ 28 & 3 \end{array}$ | rms | damp erln |  | erdp |  |
| 1329 | 1416 | 8.59059. | . 46 N | N 772 | 28.5W 14 | 52 |  | 1.16 | 0.00021 | . 617. | 5.7 |  |
| stn | dist | azm ain | w p | phas | calcph | hrmn | tsec | t-obs | t-cal | res |  | di |
| LCO | 3398 | 168.340 .0 |  |  | P | 1422 | 9.6 | 360.99 | 359.70 | 1.29 | 1.00 | 10 |
| RCBR | 4682 | 99.836 .3 |  |  | P | 1423 | 45.0 | 456.39 | 457.12 | -0.72 | 1.00 | 7 |
| PFO | 5437 | 315.833 .9 | 0 P |  | P | 1424 | 39.4 | 510.86 | 510.52 | 0.35 | 1.00 | 7 |
| EFI | 6121 | 165.431 .7 | 0 P |  | P | 1425 | 25.1 | 556.49 | 555.86 | 0.63 | 1.00 | 7 |
| EFI | 6121 | 165.4 | 0 I | IVmB_BB |  | 1425 | 28.3 | 559.7 |  |  |  |  |
| EFI | 6121 | 165.4 | 0 I | IAmb |  | 1426 | 9.7 | 601.1 |  |  |  |  |
| CMLA | 6687 | 46.129 .9 |  | P | P | 1425 | 59.1 | 590.53 | 591.50 | -0.97 | 1.00 | 2 |
| CMLA | 6687 | 46.1 | 0 I | IVmB_BB |  | 1426 | 3.6 | 595.0 |  |  |  |  |
| CMLA | 6687 | 46.1 |  | IAmb |  | 1426 | 4.2 | 595.6 |  |  |  |  |
| MACI | 7140 | 59.028 .5 |  |  | P | 1426 | 27.2 | 618.59 | 618.76 | -0.17 | 1.00 | 2 |
| MACI | 7140 | 59.0151 .0 | 0 p | pP | pP | 1427 | 3.7 | 655.14 | 654.18 | 0.96 | 1.00 | 5 |
| PAB | 8504 | 49.624 .3 |  |  | P | 1427 | 40.6 | 691.97 | 693.14 | -1.17 | 1.00 | 1 |
| PAB | 8504 | 49.6155 .3 |  |  | pP | 1428 | 18.2 | 729.56 | 729.75 | -0.19 | 1.00 | 5 |
| PAB | 8504 | 49.626 .2 |  |  | S | 1437 | 15.41 | 1266.861 | 1266.68 | 0.18 | 1.00 | 8 |
| KDAK | 9045 | 328.422 .7 |  |  | P | 1428 | 6.6 | 717.97 | 719.55 | -1.57 | 1.00 | 3 |
| BFO | 9626 | 41.820 .8 | 0 P |  | P | 1428 | 32.9 | 744.36 | 746.02 | -1.65 | 1.00 | 1 |
| BFO | 9626 | 41.8 | 0 I | IVmB_BB |  | 1428 | 37.2 | 748.6 |  |  |  |  |
| BFO | 9626 | 41.8 | 0 I | IAmb |  | 1428 | 37.9 | 749.4 |  |  |  |  |
| BFO | 9626 | 41.8158 .8 | 0 p | pP | pP | 1429 | 11.1 | 782.48 | 783.45 | -0.96 | 1.00 | 4 |
| KBS | 9899 | 11.120 .0 |  |  | P | 1428 | 45.8 | 757.23 | 757.65 | -0.42 | 1.00 | 1 |
| KBS | 9899 | 11.1 | 0 I | IAmb |  | 1428 | 49.9 | 761.4 |  |  |  |  |
| KBS | 9899 | 11.1 | 0 I | IVmB_BB |  | 1428 | 51.9 | 763.3 |  |  |  |  |
| KBS | 9899 | 11.135 .6 | 0 P | PP | PP | 1432 | 20.5 | 971.87 | 968.68 | 3.20 | 1.00 | 2 |
| KEV | 10472 | 19.719 .5 | 0 P |  | P | 1429 | 8.0 | 779.44 | 781.44 | -2.00 | 1.00 | 0 |
| KEV | 10472 | 19.7 | 0 I | IAmb |  | 1429 | 11.9 | 783.3 |  |  |  |  |
| KEV | 10472 | 19.7 | 0 I | IVmB_BB |  | 1429 | 13.5 | 784.9 |  |  |  |  |
| KEV | 10472 | 19.726 .5 | 0 S | SP | SP | 1441 | 25.81 | 1517.181 | 1514.82 | 2.36 | 1.00 | 6 |
| BILL | 10982 | 340.018 .9 | 0 P |  | Pdif | 1429 | 29.2 | 800.57 | 801.82 | -1.25 | 1.00 | 2 |
| BILL | 10982 | 340.0 | 0 I | IVmB_BB |  | 1429 | 32.3 | 803.7 |  |  |  |  |
| BILL | 10982 | 340.0 | 0 I | IAmb |  | 1429 | 35.1 | 806.5 |  |  |  |  |
| BILL | 10982 | 340.011 .7 | 0 S | SKSac | SKSac | 1439 | 53.61 | 1425.021 | 1425.40 | -0.37 | 1.00 | 4 |
| KURK | 13871 | 18.28 .0 |  |  | PKPdf | 1434 | 49.31 | 1120.701 | 1121.34 | -0.64 | 1.00 | 0 |
| NWAO | 16181 | 202.113 .2 | 0 P |  | PKPbc | 1435 | 28.61 | 1159.981 | 1160.26 | -0.28 | 1.00 | 3 |
| ENH | 16499 | 348.56 .8 | 0 P |  | PKPdf | 1435 | 33.21 | 1164.591 | 1164.16 | 0.44 | 1.00 | 1 |
| KMI | 17148 | 359.65 .9 | 0 P |  | PKPdf | 1435 | 42.81 | 1174.191 | 1173.26 | 0.94 | 1.00 | 1 |
| PALK | 17448 | 69.05 .4 | 0 P |  | PKPdf | 1435 | 45.81 | 1177.261 | 1176.64 | 0.62 | 1.00 | 1 |
| СНтO | 17812 | 10.04 .8 | 0 P | PKPdf | PKPdf | 1435 | 49.61 | 1181.041 | 1180.59 | 0.45 | 1.00 | 1 |
| СНтO | 17812 | 10.0175 .2 | 0 p | pPKPdf | pPKPdf | 1436 | 28.51 | 1219.871 | 1220.40 | -0.53 | 1.00 | 5 |
| СНтO | 17812 | 10.0177 .3 | 0 s | sPKPdf | sPKPdf | 1436 | 45.41 | 1236.841 | 1235.95 | 0.89 | 1.00 | 10 |
| KAPI | 18072 | 256.64 .2 |  |  | PKPdf | 1435 | 52.21 | 1183.621 | 1183.05 | 0.57 | 1.00 | 2 |
| 2013 | 291 | 4168.6 D |  | $.991-7$ | 77.47514 | . 5 TE | ES 19 | 1.26 .8 | 8 bTES 7. | OBTES |  |  |

Output from the location program: Adding three pP phases and one pPKPdf and sPKPdf each, the hypocenter depth changes (shown in the third and last line) from 132 to 149 km . While this is now more different from the solution given by the USGS, we take this as the best solution determined from our data set, which may be even better than the USGS solution, because the latter commonly uses only P-wave first arrivals for their hypocenter location. Yet, the reading, proper identification and time picking of later arriving phases is crucial for significantly reducing the errors in hypocenter depth estimates (see Figure below).


Left: hypocenter locations using only P phases; middle: by adding S phases; right: by adding also depth phases and core reflections. (Copy of Figure 7 from IS 11.1, modified from Schöffel and Das, J. Geophys. Res., Vol. 104, No. B6, page 13, Figure 2; © 1999, by permission of American Geophysical Union).


Map showing the epicenter of the Colombia earthquake (red star) determined by using a network of globally distributed stations (blue triangles). For comparison we plotted the epicenter from the single station (BFO, see label) 3-component location as a green star. For details of the BFO location see the next section.

## 6 Single station 3-component source location

So far we have demonstrated how data from a global network can be processed in SEISAN. This is nowadays the common procedure as the data from a large number of stations are now freely accessible via Internet. However, it is also possible with SEISAN to estimate the event location by analyzing only the three-component records of a single station. The epicentral distance of the station can be determined best from the time difference S-P, but also using time differences of P to other later phases such as PP, SP or even SS (see Fig. 11.23 of Chapter 11 in Bormann2009, and EX 11.2). SKS-P is not suitable, because this time difference does not change much with distance. The backazimuth can be determined from the amplitude ratios of the three components (see Figure 1 and text in IS 11.1 and EX 11.2). For the backazimuth calculation the method of Roberts et al. (1989) is implemented in SEISAN.

We start with the determination of the back-azimuth from the P-wave first-motion amplitudes, as we need the backazimuth to rotate the seismograms into the ZRT system, which we will use to identify the phases.


Three-component analysis of station BFO at $\Delta=86.4^{\circ}$, filtered $0.01-0.1 \mathrm{~Hz}$ : From, the above trace plot we see a positive correlation between the vertical and the two horizontal components. By definition this means that first motion direction of P in the horizontal components shows toward the source, which is in the south-west. However, since the N-S amplitude is much smaller than the E-W amplitude (compare the numbers on the outermost right side of the traces), we can further conclude that the ray is coming more from the west than from the south thus matching for station BFO a backazimuth of $262^{\circ}$.

In the next step we estimate the epicentral distance via the time difference between P and identified later arriving phases.


Three-component analysis of station BFO at $\Delta=86.4^{\circ}$, unfiltered: From the time difference between P with PP and S (here identified as SKS on the middle trace and as the slightly later arriving $S$ on the bottom trace) we estimate the epicentral distance, assuming a source depth of 150 km according to the pP-P time (see Table below). This depth estimate agrees reasonably well with interpreting the strong onsets that follow SKS. S arrives about 13 s after SKS and the depth phase sS 74 s after S, corresponding at $\Delta=86.4^{\circ}$ to a computed source depth of 170 km according to the IASP91 tables. This gives some feeling for the possible influence of errors in the assumed velocity model, phase interpretation and/or onset-time piking on the estimation of source depth.

We can either read the distance for which we get the best match between our observations and the travel time curves of the global IASP91 velocity model, or equivalently estimate it with a grid search by computing travel times for a range of distances as done here. In our example we then get $\Delta=86.5^{\circ}$ (see Table below). This differs only $0.15^{\circ}$ from our first multi-station P-wave location ( $86.35^{\circ}$ ) and even less from our improved multi-station and multi-phase location ( $86.56^{\circ}$ ) (see above location program outputs). Together with the backazimuth we can now locate the event on a suitable stereographic map with station BFO in the center (as in Figure 12 of EX 11.2 for an Ecuador earthquake and station CLL).

| Phase difference | Time difference $\boldsymbol{\delta t}(\mathbf{s})$ | $\boldsymbol{\delta t}(\mathbf{s})$ for $\Delta=\mathbf{8 6}^{\circ}$ | $\boldsymbol{\delta t}(\mathbf{s})$ for $\Delta=\mathbf{8 7}^{\circ}$ |
| :---: | :---: | :---: | :---: |
| PP-P | 205.7 | 202 | 205 |
| S-P | 623.3 | 622 | 626 |



Output from the location program: We can obtain a single-station three-component location, which is within 500 km from the one obtained by the standard location program with several stations. While our distance estimate is very good, we would have to get a $5^{\circ}$ larger backazimuth reading to get a location very close to the multi-station location. This shows the approximate range of uncertainty of single station locations in the far teleseismic range. Wrong phase interpretation may increase single station location errors. E.g., when interpreting in this case the earlier arriving SKS as S, the distance estimate from S-P would be $0.2^{\circ}$ shorter in the case of BFO but this underestimation would increase for any station further away within the distance range where SKS arrives before S (see differential travel-time curve in Figure 4 of EX 11.2). For shallow earthquakes at $\Delta=100^{\circ}$ the error $\delta \Delta$ would reach already $0.9^{\circ}$. However, with proper S-P times, or when several other phases have also been correctly identified, the distance can generally be estimated, up to $160^{\circ}$, within $1-2^{\circ}$ and the azimuth with P-wave first motion amplitudes, when measured with good signal-to-noise ratio on well calibrated 3-component seismometer components, within about 5-10 ${ }^{\circ}$. This allows rather fast and reasonably good first location estimates even with single station data only (see Fig. 11.23 in Chapter 11 of NMSOP-1 in Bormann, 2009, and examples in EX 11.2).

Finally, we determine the teleseismic magnitudes for this earthquake. Since this is a deep earthquake, only the two teleseismic standard body-wave magnitudes mb and mB _BB should be calculated. Note, however, that the IASPEI WG on magnitudes encourages stations to measure according to the standard procedures also IAMs_20 and IVMs_BB with their periods if surface-waves are still clearly visible in records of deeper earthquakes as this is the case also for our example (see, e.g., in section 5, the record trace for station KADAK in the plot: Vertical-component traces for which phases are picked, filtered 0.02-5 Hz). Such data are of great interest for investigating the depth and period dependence of surface waves and to derive improved calibration functions $\sigma(\Delta, \mathrm{h}, \mathrm{T})$. Note that for 20 s surface-waves and thus Ms_20 calculation such depth corrections have already been published by Herak et al. (2001):

$$
\begin{aligned}
& \Delta \mathrm{Ms}(\mathrm{~h})=0 \\
& \Delta \mathrm{Ms}(\mathrm{~h})=0.314 \log (\mathrm{~h})-0.409 \\
& \Delta \mathrm{Ms}(\mathrm{~h})=1.351 \log (\mathrm{~h})-2.253 \\
& \Delta \mathrm{Ms}(\mathrm{~h})=0.400 \log (\mathrm{~h})-0.350
\end{aligned}
$$

for $\mathrm{h}<20 \mathrm{~km}$
for $20 \mathrm{~km} \leq \mathrm{h}<60 \mathrm{~km}$
for $60 \mathrm{~km} \leq \mathrm{h}<100 \mathrm{~km}$
for $100 \mathrm{~km} \leq \mathrm{h}<600 \mathrm{~km}$.
For station KDAK, e.g., one would measure IAMs_20 $=10078 \mathrm{~nm}$ at $\mathrm{T}=19 \mathrm{~s}$ and thus get a depth corrected Ms_20 $=6.2+0.5=6.7$ which compares rather well with our body-wave magnitudes $\mathrm{mb}=6.8$ and $\mathrm{mB} \_\mathrm{BB}=7.0$ determined in the following.


Amplitude reading for mb magnitude at station CMLA at $\Delta=59.9^{\circ}$ : As in the case of the regional event, the upper broadband trace is converted into a WWSSN short period trace (lower trace) on which the amplitude IAmb is read, here as 1148 nm with a period of 2.3 s .


Amplitude reading for $m B \_B B$ magnitude at station CMLA at $\Delta=59.9^{\circ}$ : As in the case of the regional event the amplitude IVmB _BB is read on the bottom trace that has been deconvolved into a broadband velocity trace (top trace shows uncorrected data, which are in the case of a broadband seismometer also proportional to velocity): here $36758 \mathrm{~nm} / \mathrm{s}$ with a period of 2.5 s .

Computing the average magnitudes from all station amplitude observations we get the values below. In this case mB _ BB is equal to Mw , and mb is only slightly smaller. Since the period at which mb is read is almost the same as for mB _ BB the difference is mainly due to the larger bandwidth of the broadband record.

| Magnitude scale | Value |
| :--- | :--- |
| Mw (USGS) | 7.0 |
| mb | 6.8 |
| mB_BB | 7.0 |

The following station amplitude readings were used in the event magnitude computation:

| EFI | BZ | dist: | 6121.0 | amp: | $13012.5 \mathrm{~T}:$ | 2.7 | $\mathrm{mB}=$ | 6.9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| EFI | BZ | dist: | 6121.0 | amp: | 788.3 T : | 1.1 | mb | 6.5 |
| CMLA | BZ | dist: | 6687.0 | amp : | 36756.6 T : | 2.5 | mb | 7.9 |
| CMLA | BZ | dist: | 6687.0 | amp: | 36758.8 T : | 2.5 | mB | 7.5 |
| CMLA | BZ | dist: | 6687.0 | amp: | 16414.7 T : | 2.3 | mb | 7.6 |
| KEV | BZ | dist: | 10472.0 | amp: | 83.5 T : | 0.8 | mb | 6.0 |
| KEV | BZ | dist: | 10472.0 | amp: | 2421.2 T: | 5.5 | $\mathrm{mB}=$ | 6.6 |
| KBS | BZ | dist: | 9899.0 | amp: | 500.9 T : | 0.9 | mb | 6.5 |
| KBS | BZ | dist: | 9899.0 | amp: | 11474.4 T : | 7.2 | $\mathrm{mB}=$ | 7.1 |
| BFO | BZ | dist: | 9626.0 | amp: | 34897.1 T: | 3.7 | $\mathrm{mB}=$ | 7.4 |
| BFO | BZ | dist: | 9626.0 | amp: | 1747.1 T: | 1.1 | $\mathrm{mb}=$ | 6.9 |
| BILL | BZ | dist: | 10982.0 | amp: | 1555.7 T : | 6.0 | $\mathrm{mB}=$ | 6.7 |
| BILL | BZ | dist: | 10982.0 | amp: | 106.9 T : | 1.2 | $\mathrm{mb}=$ | 6.3 |

## 7 Concluding remarks

The examples given here are meant to illustrate how the data processing is done using the SEISAN software and to illustrate some basic concepts of earthquake data processing. The examples should help newcomers to earthquake data processing to get started. It will be necessary to first learn SEISAN, but then the data used can be downloaded and the steps shown here followed. When analyzing seismograms, the number of phases that can be read depends on the earthquake size and thus the SNR of the recording, the epicentral distance, the source depth as well as on the bandwidth and period range of the seismic records (see Figs. 2.57-2.61 in Chapter 2). From a scientific perspective we wish to have as many good phases read as possible. However, there is often a limitation of how much can be done due to time constraints. We encourage the reader to read more than the first arriving $P$, and at least to identify clear additional later phases. A good exercise is to download data from the IRIS Wilber, take the data into SEISAN and start processing.

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